Package: lmw (via r-universe)

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Type Package

Title Linear Model Weights

Version 0.0.2

Description Computes the implied weights of linear regression models for estimating average causal effects and provides diagnostics based on these weights. These diagnostics rely on the analyses in Chattopadhyay and Zubizarreta (2023) <doi:10.1093/biomet/asac058> where several regression estimators are represented as weighting estimators, in connection to inverse probability weighting. 'lmw' provides tools to diagnose representativeness, balance, extrapolation, and influence for these models, clarifying the target population of inference. Tools are also available to simplify estimating treatment effects for specific target populations of interest.

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BugReports https://github.com/ngreifer/lmw/issues

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Contents

`influence.lmw` *Regression Diagnostics for* `lmw` *and* `lmw_est` *objects*

Description

`influence()` produces influence measures for `lmw` objects that can be used as regression diagnostics to identify influential cases. These functions produce similar outputs to `lm.influence()` but also include the sample influence curve (SIC) values, which combine information about the hat values, residuals, and implied regression weights.

Usage

```
## S3 method for class 'lmw'
influence(model, outcome, data = NULL, ...)

## S3 method for class 'lmw_est'
influence(model, ...)
```

Arguments

`model`	an `lmw` or `lmw_est` object; the output of a call to `lmw()` or `lmw_est()`.
`outcome`	the name of the outcome variable. Can be supplied as a string containing the name of the outcome variable or as the outcome variable itself. If not supplied, the outcome variable in the `formula` supplied to `lmw()`, if any, will be used.
`data`	an optional data frame containing the outcome variable named in `outcome`.
`...`	ignored.

Details

`influence()` computes the hat values, (weighted) residuals, and sample influence curve (SIC) values for each unit, which can be used as regression diagnostics to assess influence. The weighted residuals are weighted by the sampling weights (if supplied), not the implied regression weights. The SIC values are computed as `SIC = (N-1) * w * r / (1 - h)`, where `N` is the sample size, `w` are the units' implied regression weights, `r` are the (weighted) residuals, and `h` are the hat values. SIC values are scaled to have a maximum of 1. Higher values indicate greater relative influence.

Value

A list with the following components:

`hat`	a vector containing the diagonal of the hat matrix.
`wt.res`	a vector of (weighted) residuals.
`sic`	a vector containing the scaled SIC values.

Note

`influence.lmw()` uses non-standard evaluation to interpret its `outcome` argument. For programmers who wish to use `influence.lmw()` inside other functions, an effective way to pass the name of an arbitrary outcome (e.g., `y` passed as a string) is to use `do.call()`, for example:

```
fun <- function(m, y, d) {
do.call("influence", list(m, y, d)) }
```

When using `influence.lmw()` inside `lapply()` or `purrr::map` to loop over outcomes, this syntax must be used as well.

See Also

`plot.lmw()` for plotting the SIC values; `lm.influence()` for influence measures for `lm` objects, which do not include SIC values; `hatvalues()` for hat values for `lm` objects (note that `lmw_est` objects also have a `hatvalues()` method).

Examples

```
data("lalonde")

# URI regression for ATT
lmw.out1 <- lmw(~ treat + age + education + race + married +
                    nodegree + re74 + re75,
                data = lalonde, estimand = "ATT",
                method = "URI", treat = "treat")

# Influence for re78 outcome
infl <- influence(lmw.out1, outcome = "re78")
str(infl)

# Can also be used after lmw_est():
lmw.est1 <- lmw_est(lmw.out1, outcome = "re78")
```

```
all.equal(infl,
          influence(lmw.est1))
```

`lalonde` *Data from National Supported Work Demonstration and PSID, as analyzed by Dehejia and Wahba (1999).*

Description

This is a subsample of the data from the treated group in the National Supported Work Demonstration (NSW) and the comparison sample from the Population Survey of Income Dynamics (PSID). This data was previously analyzed extensively by Lalonde (1986) and Dehejia and Wahba (1999). The original dataset is available at https://users.nber.org/~rdehejia/nswdata2.html.

Usage

```
lalonde
```

Format

A data frame with 2675 observations (185 treated, 2490 control). There are 9 variables measured for each individual. In addition, two constructed variables are included: `treat_multi`, which splits the original control group into two, and `Ins`, which is a constructed instrumental variable.

- "treat" is the treatment assignment (1=treated, 0=control).
- "age" is age in years.
- "education" is education in number of years of schooling.
- "race" is the individual's race/ethnicity, (Black, Hispanic, or White).
- "married" is an indicator for married (1=married, 0=not married).
- "nodegree" is an indicator for whether the individual lacks a high school degree (i.e., has fewer than 12 years of schooling; 1=no degree, 0=degree).
- "re74" is income in 1974, in U.S. dollars.
- "re75" is income in 1975, in U.S. dollars.
- "re78" is income in 1978, in U.S. dollars.
- "treat_multi" is a constructed version of "treat" that splits the control group into to levels (1=treated, 2=control group A, 3=control group B).
- "Ins" is a binary instrumental variable.

"treat" is the treatment variable, "re78" is the outcome, and the others are pre-treatment covariates. Note that in the original data, "race" is instead coded as two dummy variables, "black" and "hispan".

Details

The data corresponds to the NSW treated sample and the PSID control sample with 1974 earnings included. This specific dataset is different from the one in the **MatchIt** and **cobalt** packages, which is a subset of this dataset.

References

Lalonde, R. (1986). Evaluating the econometric evaluations of training programs with experimental data. American Economic Review 76: 604-620.

Dehejia, R.H. and Wahba, S. (1999). Causal Effects in Nonexperimental Studies: Re-Evaluating the Evaluation of Training Programs. Journal of the American Statistical Association 94: 1053-1062.

`lmw` *Compute linear regression-implied weights*

Description

Computes the weights implied by a linear outcome regression model that would estimate a weighted difference in outcome means equal to the covariate-adjusted treatment effect resulting from the supplied regression model.

Usage

```
lmw(
  formula,
  data = NULL,
  estimand = "ATE",
  method = "URI",
  treat = NULL,
  base.weights = NULL,
  s.weights = NULL,
  dr.method = "WLS",
  obj = NULL,
  fixef = NULL,
  target = NULL,
  target.weights = NULL,
  contrast = NULL,
  focal = NULL
)
```

Arguments

`formula`	a one-sided formula with the treatment and covariates on the right-hand side corresponding to the outcome regression model to be fit. The outcome variable is not involved in computing the weights and does not need to be specified. See Details for how this formula is interpreted in light of other options.
`data`	a data frame containing the variables named in `formula` and `treat`.
`estimand`	the estimand of interest, which determines how covariates are centered. Should be one of `"ATE"` for the average treatment effect, `"ATT"` for the average treatment effect in the treated, `"ATC"` for the average treatment effect in the control, or `"CATE"` for the conditional average treatment effect. When `estimand = "CATE"`, an argument to `target` must be supplied. This argument also affects

what summary.lmw() considers to be the target population. Default is "ATE" unless obj is specified, in which case it takes its value from the supplied object.

method — the method used to estimate the weights; either "URI" (the default) for uni-regression imputation weights, where a single model is fit to the whole dataset, or "MRI" for multi-regression imputation, where the model is fit separately in the treatment groups. This affects the interpretation of formula. See Details.

treat — the name of the treatment variable in data. If unspecified, the first variable present in formula will be taken as the treatment variable with a message. See Details.

base.weights — a vector of base weights. See Details. If omitted and obj is specified, the weights from the supplied object will be used. Can be supplied as a numeric vector, a string containing the name of the variable in data containing the base weights, or the unquoted name of the variable in data containing the base weights.

s.weights — a vector of sampling weights. See Details. If omitted and obj is specified, the sampling weights from the supplied object will be used. Can be supplied as a numeric vector, a string containing the name of the variable in data containing the sampling weights, or the unquoted name of the variable in data containing the sampling weights.

dr.method — the method used to incorporate the base.weights into a doubly-robust estimator. Can be one of "WLS" for weighted least squares ("IPWRA" is an allowable alias) or "AIPW" for augmented inverse probability weighting. Ignored when base.weights is NULL.

obj — a matchit or weightit object corresponding to the matched or weighted sample in which the implied outcome regression would take place. See Details.

fixef — optional; a string or one-sided formula containing the name of the fixed effects variable in data. See Details. Cannot be used with dr.method = "AIPW".

target — a list or data frame containing the target values for each covariate included in formula. Ignored with a warning when estimand is not "CATE". See Details.

target.weights — a vector of sampling weights to be applied to target when supplied as a data frame. Ignored with a warning when estimand is not "CATE". See Details.

contrast — for multi-category treatments with method = "URI", a vector containing the names or indices of the two treatment levels to be contrasted (since in this case the weights depend on the specific contrast). See Details.

focal — the level of the treatment variable to be considered "focal" (i.e., the "treated" level when estimand = "ATT" or the control level when estimand = "ATC"). Ignored when estimand is "ATE" or "CATE". Otherwise, if unspecified, the second value of contrast will be considered focal when estimand = "ATT" and the first value of contrast will be considered focal when estimand = "ATC". For binary treatments, this generally does not need to be supplied. See Details.

Details

formula is interpreted differently depending on whether method is "URI" or "MRI". When method = "URI", the formula is taken literally as the right-hand side of the outcome model formula. The only difference is that the covariates will be centered based on the argument to estimand (see below). When method = "MRI", all references to the treatment are removed (i.e., covariate interactions

with treatment become covariate main effects if not already present), and the new formula is taken as the right-hand side of the model formula fit within each treatment group. This is equivalent to allowing all covariates to have both main effects and interactions with treatment after centering the covariates based on the argument to `estimand`. Allowing the treatment to interact with all covariates with `method = "URI"` is equivalent to specifying `method = "MRI"`, and, for binary treatments, the returned weights will be the same when `fixef = NULL`.

When any treatment-by-covariate interactions are present in `formula` or when `method = "MRI"`, covariates are centered at specific values to ensure the resulting weights correspond to the desired estimand as supplied to the `estimand` argument. For the ATE, the covariates are centered at their means in the full sample. For the ATT and ATC, the covariates are centered at their means in the treatment or control group (i.e., the `focal` group), respectively. For the CATE, the covariates are centered according to the argument supplied to `target` (see below). Note that when covariate-by-covariate interactions are present, they will be centered after computing the interaction rather than the interaction being computed on the centered covariates unless `estimand = "CATE"`, in which case the covariates will be centered at the values specified in `target` prior to involvement in interactions.

Estimating a CATE:

When `estimand = "CATE"`, `target` can be supplied either as a single target profile (i.e., a list or a data frame with one row) or as a target dataset, potentially with its own sampling weights, which are supplied to `target.weights`. The variables included in `target` must correspond to all the named *covariates* in `formula`; for example, if `formula = ~ X1 + log(X1) + X2 + X1:X2`, values in `target` must be given for `X1` and `X2`, but not `log(X1)` or `X1:X2`. To choose a target profile value for a factor corresponding to a proportion (e.g., a target value of .5 for a variable like `sex` indicating a target population with a 50-50 sex split), the factor variable must be split into a numeric variable beforehand, e.g., using `model.matrix()` or `cobalt::splitfactor()`. `target` values cannot be given to variables specified using `$`, `[[]]`, or `[]` (e.g., `data$X1`), so an error will be thrown if they are used in `formula`. When a target dataset is supplied, covariates will be centered at their means in the (`target.weights`-weighted) target dataset.

Base weights and sampling weights:

Base weights (`base.weights`) and sampling weights (`s.weights`) are similar in that they both involve combining weights with an outcome regression model. However, they differ in a few ways. Sampling weights are primarily used to adjust the target population; when the outcome model is fit, it is fit using weighted least squares, and when target balance is assessed, it is assessed using the sampling weighted population as the target population. Centering of covariates in the outcome model is done using the sampling weighted covariate means. Base weights are primarily used to offer a second level of balancing beyond the implied regression weights; they can be incorporated into the effect estimate either using weighted least squares or using the augmented inverse probability weighting (AIPW) estimator. Base weights do not change the target population, so when target balance is assessed, it is assessed using the unweighted population as the target population.

Some forms of weights both change the target population and provide an extra layer of balancing, like propensity score weights that target estimands other than the ATT, ATC, or ATE (e.g., overlap weights), or matching weights where the target population is defined by the matching (e.g., matching with a caliper, cardinality matching, or coarsened exact matching). Because these weights change the target population, they should be supplied to `s.weights` to ensure covariates are appropriately centered. When there are no treatment-by-covariate interactions and `method = "URI"`, whether weights are supplied to `base.weights` or `s.weights` will not matter for the estimation of the weights but will affect the target population in balance assessment.

When both base.weights and s.weights are supplied, e.g., when the base weights are the result of a propensity score model fit with sampling weights, it is assumed the base weights do not incorporate the sampling weights; that is, it is assumed that to estimate a treatment effect *without* regression adjustment, the base weights and the sampling weights would have to be multiplied together. This is true, for example, for the weights in a matchit or weightit object (see below) but not for weights in the output of MatchIt::match.data() unless called with include.s.weights = FALSE or weights resulting from CBPS::CBPS().

Regression after using MatchIt or WeightIt:

Regression weights can be computed in a matched or weighted sample by supplying a matchit or weightit object (from **MatchIt** or **WeightIt**, respectively) to the obj argument of lmw(). The estimand, focal group (if any), base weights, and sampling weights (if any) will be taken from the supplied object and used in the calculation of the implied regression weights, unless these have been supplied separately to lmw(). The weights component of the supplied object containing the matching or balancing weights will be passed to base.weights and the s.weights component will be passed to s.weights. Arguments supplied to lmw() will take precedence over the corresponding components in the obj object.

Multi-category treatments:

There are a few differences when the treatment has multiple (i.e., more than 2) categories. If estimand is "ATT" or "ATC", an argument should be supplied to focal identifying which group is the treated or control (i.e., "focal") group, respectively.

The key difference, though, is when method = "URI", because in this case the contrast between each pair of treatment groups has its own weights and its own implied target population. Because lmw() only produces one set of weights, an argument must be supplied to contrast identifying which groups are to be used as the contrast for computing the weights. In addition, to compute the treatment effect corresponding to the chosen contrast as a weighted difference in outcome means, the difference must be taken between the weighted mean of the non-reference group and the weighted mean of *all other groups combined*, rather than simply the weighted mean of the reference group.

The implication of this is that contrast statistics computed in the weighted sample involve all units, even those not in the contrasted groups, whereas statistics computed in the unweighted sample only involve units in the contrasted groups. See summary.lmw() for more information on assessing balance using the regression weights for multi-category treatments. Given these complications, it is generally best to use method = "MRI" with multi-category treatments.

Fixed effects:

A fixed effects variable can be supplied to the fixef argument. This is equivalent to adding the fixed effects variable as a predictor that does not interact with the treatment or any other covariate. The difference is that computation is much faster when the fixed effect has many levels because demeaning is used rather than including the fixed effect variable as a collection of dummy variables. When using URI, the weights will be the same regardless of whether the fixed effect variable is included as a covariate or supplied to fixef; when using MRI, results will differ because the fixed effect variable does not interact with treatment. The fixed effects variable will not appear in the summary.lmw() output (but can be added using addlvariables argument) or in the model output of lmw_est() or summary.lmw_est(). Because it does not interact with the treatment, the distribution of the fixed effect variable may not correspond to the target population, so caution should be used if it is expected the treatment effect varies across levels of this variable

(in which case it should be included as a predictor). Currently only one fixed effect variable is allowed.

Value

An `lmw` object, which contains the following components:

`treat`	the treatment variable, given as a factor.
`weights`	the computed implied regression weights.
`covs`	a data frame containing the covariates included the model formula.
`estimand`	the requested estimand.
`method`	the method used to estimate the weights (`"URI"` or `"MRI"`).
`base.weights`	the weights supplied to `base.weights`.
`s.weights`	the weights supplied to `s.weights`.
`dr.method`	when `base.weights` are supplied, the method for computing the doubly-robust weights.
`call`	the original call to `lmw()`.
`fixef`	the fixed effects variable if supplied to `fixef`.
`formula`	the model formula.
`target`	the supplied target profile or dataset when `estimand = "CATE"`, after some initial processing. The `"target.weights"` attribute contains the `target.weights` if supplied.
`contrast`	the contrasted treatment groups.
`focal`	the focal treatment level when `estimand` is `"ATT"` or `"ATC"`.

References

Chattopadhyay, A., & Zubizarreta, J. R. (2023). On the implied weights of linear regression for causal inference. *Biometrika*, 110(3), 615–629. doi:10.1093/biomet/asac058

See Also

`summary.lmw()` for summarizing balance and representativeness; `plot.lmw()` for plotting features of the weights; `lmw_est()` for estimating treatment effects from `lmw` objects; `influence.lmw()` for influence measures; `lm()` for fitting standard regression models.

Examples

```
data("lalonde")

# URI regression for ATT
lmw.out1 <- lmw(~ treat + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                estimand = "ATT", method = "URI",
                treat = "treat")
lmw.out1
```

```
summary(lmw.out1)

# MRI regression for ATT
lmw.out2 <- lmw(~ treat + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                estimand = "ATT", method = "MRI",
                treat = "treat")
lmw.out2
summary(lmw.out2)


# MRI regression for ATT after propensity score matching
m.out <- MatchIt::matchit(treat ~ age + education + race +
                            married + nodegree + re74 + re75,
                          data = lalonde, method = "nearest",
                          estimand = "ATT")
lmw.out3 <- lmw(~ treat + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                method = "MRI", treat = "treat", obj = m.out)
lmw.out3
summary(lmw.out3)

# MRI regression for CATE with given target profile
target.prof <- list(age = 25, education = 11, race = "black",
                    married = 0, nodegree = 1, re74 = 0,
                    re75 = 0)
lmw.out4 <- lmw(~ treat + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                estimand = "CATE", method = "MRI",
                treat = "treat", target = target.prof)
lmw.out4
summary(lmw.out4)

# MRI regression for CATE with given target dataset (in
# this case, will give the same as with estimand = "ATT")
target.data <- subset(lalonde, treat == 1)
lmw.out4 <- lmw(~ treat + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                estimand = "CATE", method = "MRI",
                treat = "treat", target = target.data)
lmw.out4
summary(lmw.out4)

# URI regression with fixed effects for 'race'
lmw.out5 <- lmw(~ treat + age + education + married +
                  nodegree + re74 + re75, data = lalonde,
                method = "URI", treat = "treat",
                fixef = ~race)
lmw.out5

# Produces the same weights as when included as a covariate
all.equal(lmw.out1$weights, lmw.out5$weights)
```

```
# MRI for a multi-category treatment, ATT with 1 as the focal
# group
lmw.out6 <- lmw(~ treat_multi + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                estimand = "ATT", method = "MRI",
                treat = "treat_multi", focal = "1")
lmw.out6
summary(lmw.out6)

# URI for a multi-category treatment; need to specify
# contrast because only two groups can be compared at
# a time
lmw.out7 <- lmw(~ treat_multi + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                estimand = "ATE", method = "URI",
                treat = "treat_multi", contrast = c("2", "3"))
lmw.out7
summary(lmw.out7)
```

`lmw_est` *Estimate a treatment effect from a linear model*

Description

`lmw_est()` fits the outcome regression corresponding to the model used to compute the weights in the supplied `lmw` object and returns the model coefficients and their covariance matrix. Use `summary.lmw_est()` to compute and view the treatment effect and potential outcome mean estimates and their standard errors.

Usage

```
lmw_est(x, ...)

## S3 method for class 'lmw'
lmw_est(x, outcome, data = NULL, robust = TRUE, cluster = NULL, ...)

## S3 method for class 'lmw_aipw'
lmw_est(x, outcome, data = NULL, robust = TRUE, cluster = NULL, ...)

## S3 method for class 'lmw_iv'
lmw_est(x, outcome, data = NULL, robust = TRUE, cluster = NULL, ...)
```

Arguments

`x`	an `lmw` or `lmw_iv` object; the output of a call to `lmw()` or `lmw_iv()`.
`...`	other arguments passed to `sandwich::vcovHC()` or `sandwich::vcovCL()`.

`outcome` the name of the outcome variable. Can be supplied as a string containing the name of the outcome variable or as the outcome variable itself. If not supplied, the outcome variable in the `formula` supplied to `lmw()` or `lmw_iv()`, if any, will be used.

`data` an optional data frame containing the outcome variable named in `outcome` and the cluster variable(s) when `cluster` is supplied as a `formula`.

`robust` whether to compute the robust covariance matrix for the model coefficients. Allowable values include those allowed for the `type` argument of `sandwich::vcovHC()` or `sandwich::vcovCL()` when `cluster` is specified. Can also be specified as `TRUE` (the default), which means `"HC3"` or `"HC1"` when `cluster` is specified, or `FALSE`, which means `"const"` (i.e., the standard non-robust covariance). When `cluster` is specified, `robust` will be set to `TRUE` if `FALSE`. When AIPW is used, `robust` is ignored; the HC0 robust covariance matrix is used.

`cluster` the clustering variable(s) for computing a cluster-robust covariance matrix. See `sandwich::vcovCL()`. If supplied as a `formula`, the clustering variables must be present in the original dataset used to compute the weights or `data`. When AIPW is used, `cluster` is ignored.

Details

`lmw_est()` uses `lm.fit()` or `lm.wfit()` to fit the outcome regression model (and first stage model for `lmw_iv` objects) and returns the output of these functions augmented with other components related to the estimation of the weights. Unlike with `lm.[w]fit()`, the covariance matrix of the parameter estimates is also included in the output.

For `lmw` objects, the model fit is that supplied to the `formula` input to `lmw()` except that it is fit in a dataset appropriately centered to ensure the estimand corresponds with the one requested. When `method = "MRI"` in the call to `lmw()`, the model is fit as an interaction between the treatment and all the (centered) terms in the model formula. The results will be similar to those from using `lm()` on this model and supplied data except that the covariates are centered beforehand. The product of the sampling weights and base weights supplied to `lmw()`, if any, will be supplied to `lm.wfit()` to fit the model using weighted least squares.

For `lmw_aipw` objects, the model is fit as above except that base weights are not included in the model fitting and are instead used to compute additional augmentation terms that are added to the estimated potential outcome means from the outcome regression. The variance-covariance matrix is computed using M-estimation; this corresponds to the HC0 robust covariance matrix for the model parameters with the base weights treated as fixed, which yields conservative standard errors for the ATE. Inference is only approximate for the ATT and ATC.

For `lmw_iv` objects, the first stage model is constructed by removing the treatment from the supplied model formula, adding the instrumental variable as a main effect, and using the treatment variable as the outcome. For the second stage (reduced form) model, the fitted values of the treatment from the first stage model are used in place of the treatment in the outcome model. The results are similar to those from using `ivreg::ivreg()`, and the coefficients estimates will be the same except for the intercept due to the centering of covariates.

Although some coefficients in the model may be interpretable as treatment effect estimates, `summary.lmw_est()` should be used to view and extract the treatment effect and potential outcome mean estimates, standard errors, and other model statistics. The output of `lmw_est()` should rarely be used except to be supplied to `summary()`.

Value

An lmw_est object with the following components:

coefficients, residuals, fitted.values, effects, weights, rank, df.residual, qr
: for lmw objects, the output of the lm.fit() or lm.wfit() call used to fit the outcome model. For lmw_iv objects, the output of the lm.fit() or lm.wfit() call used to fit the the second stage model, with residuals corresponding to the residuals computed when substituting the true treatment variable in place of the fitted treatment values in the model.

model.matrix
: the model matrix (supplied to the x argument of lm.fit).

vcov
: the estimated covariance matrix of the parameter estimates as produced by sandwich::vcovHC() or sandwich::vcovCL().

lmw.weights
: the implied regression weights computed by lmw_est().

call
: the call to lmw_est().

estimand
: the requested estimand.

focal
: the focal treatment level when estimand is "ATT" or "ATC".

method
: the method used to estimate the weights ("URI" or "MRI").

robust
: the type standard error used.

outcome
: the name of the outcome variable.

treat_levels
: the levels of the treatment.

When AIPW is used, the object will be of class lmw_est_aipw, which inherits from lmw_est, and contains the additional components:

coef_aipw
: the model-predicted potential outcome means (mu) and the augmentation terms (aug).

vcov_aipw
: the covariance matrix of the quantities in coef_aipw.

When weights are included in the estimation (i.e., base.weights or s.weights supplied to lmw() or lmw_iv()), any units will weights equal to zero will be removed from the data prior to model fitting.

Methods exist for lmw_est objects for model.matrix(), vcov(), hatvalues(), sandwich::bread(), and sandwich::estfun(), all of which are used internally to compute the parameter estimate covariance matrix. The first two simply extract the corresponding component from the lmw_est object and the last three imitate the corresponding methods for lm objects (or ivreg objects for lmw_iv inputs). Other regression-related functions, such as coef(), residuals(), and fitted(), use the default methods and should work correctly with lmw_est objects.

Note that when fixed effects are supplied through the fixef argument to lmw() or lmw_iv(), standard error estimates computed using functions outside **lmw** may not be accurate due to issues relating to degrees of freedom. In particular, this affects conventional and HC1-robust standard errors. Otherwise, sandwich::vcovHC() can be used to compute standard errors (setting type = "const" for conventional standard errors), though sandwich::vcovCL() may not work as expected and should not be used. To calculate cluster-robust standard errors, supply an argument to cluster in lmw_est().

Note

`lmw_est()` uses non-standard evaluation to interpret its `outcome` argument. For programmers who wish to use `lmw_est()` inside other functions, an effective way to pass the name of an arbitrary outcome (e.g., `y` passed as a string) is to use `do.call()`, for example:

```
fun <- function(model, outcome, data) {
do.call("lmw_est", list(model, outcome, data)) }
```

When using `lmw_est()` inside `lapply()` or `purrr::map` to loop over outcomes, this syntax must be used as well.

See Also

`summary.lmw_est()` for viewing and extracting the treatment effect and potential outcome mean estimates, standard errors, and other model statistics; `lmw()` or `lmw_iv()` for estimating the weights that correspond to the model estimated by `lmw_est()`; `lm()` and `lm.fit()` for fitting the corresponding model; `ivreg()` in the **ivreg** package for fitting 2SLS models; `influence.lmw_est()` for influence measures

Examples

```
data("lalonde")

# MRI regression for ATT
lmw.out1 <- lmw(~ treat + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                  estimand = "ATT", method = "MRI",
                  treat = "treat")

lmw.fit1 <- lmw_est(lmw.out1, outcome = "re78")
lmw.fit1

summary(lmw.fit1)


# MRI regression for ATT after propensity score matching
m.out <- MatchIt::matchit(treat ~ age + education + race +
                            married + nodegree + re74 + re75,
                          data = lalonde, method = "nearest",
                          estimand = "ATT")
lmw.out2 <- lmw(~ treat + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                method = "MRI", treat = "treat", obj = m.out)

## Using a cluster-robust SE with subclass (pair membership)
## as the cluster variable
lmw.fit2 <- lmw_est(lmw.out2, outcome = "re78", cluster = ~subclass)
lmw.fit2

summary(lmw.fit2)
```

```
# AIPW for ATE with MRI regression after propensity score
# weighting
ps <- glm(treat ~ age + education + race + married + nodegree +
            re74 + re75, data = lalonde,
            family = binomial)$fitted
ipw <- ifelse(lalonde$treat == 1, 1/ps, 1/(1-ps))

lmw.out3 <- lmw(re78 ~ treat + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                method = "MRI", treat = "treat",
                base.weights = ipw, dr.method = "AIPW")
lmw.fit3 <- lmw_est(lmw.out3)
lmw.fit3

summary(lmw.fit3)

# MRI for multi-category treatment ATE
lmw.out3 <- lmw(~ treat_multi + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                estimand = "ATE", method = "MRI",
                treat = "treat_multi")
lmw.fit3 <- lmw_est(lmw.out3, outcome = "re78")
lmw.fit3

summary(lmw.fit3)
```

`lmw_iv` *Compute instrumental variable regression-implied weights*

Description

Computes the weights implied by an instrumental variable (IV) model that would estimate a weighted difference in outcome means equal to the treatment effect resulting from the supplied model fit with two-stage least squares.

Usage

```
lmw_iv(
  formula,
  data = NULL,
  estimand = "ATE",
  method = "URI",
  treat = NULL,
  iv,
  base.weights = NULL,
  s.weights = NULL,
  obj = NULL,
  fixef = NULL,
  target = NULL,
```

```
  target.weights = NULL,
  contrast = NULL,
  focal = NULL
)
```

Arguments

formula	a one-sided formula with the treatment and covariates on the right-hand side corresponding to the second-stage (reduced form) outcome regression model to be fit. If an outcome variable is supplied on the left-hand side, it will be ignored. This model should not include an IV. See Details for how this formula is interpreted in light of other options.
data	a data frame containing the variables named in formula, treat, and iv.
estimand	the estimand of interest, which determines how covariates are centered. Should be one of "ATE" for the average treatment effect, "ATT" for the average treatment effect in the treated, "ATC" for the average treatment effect in the control, or "CATE" for the conditional average treatment effect. When estimand = "CATE", an argument to target must be supplied. This argument also affects what summary.lmw() considers to be the target population. Default is "ATE" unless obj is specified, in which case it takes its value from the supplied object.
method	the method used to estimate the weights; either "URI" (the default) for uni-regression imputation weights, where a single model is fit to the whole dataset, or "MRI" for multi-regression imputation, where the covariates fully interact with the treatment. This affects the interpretation of formula. See Details.
treat	the name of the treatment variable in data. If unspecified, the first variable present in formula will be taken as the treatment variable with a message. Currently, only binary treatments are supported. See Details.
iv	a character vector or one-sided formula containing the names of the IVs in data. These variables should not appear in formula. Multiple IVs are allowed. See Details. This argument is required.
base.weights	a vector of base weights. See Details. If omitted and obj is specified, the weights from the supplied object will be used. Can be supplied as a numeric vector, a string containing the name of the variable in data containing the base weights, or the unquoted name of the variable in data containing the base weights.
s.weights	a vector of sampling weights. See Details. If omitted and obj is specified, the sampling weights from the supplied object will be used. Can be supplied as a numeric vector, a string containing the name of the variable in data containing the sampling weights, or the unquoted name of the variable in data containing the sampling weights.
obj	a matchit or weightit object corresponding to the matched or weighted sample in which the implied IV regression would take place. See Details.
fixef	optional; a string or one-sided formula containing the name of the fixed effects variable in data. See Details.
target	a list or data frame containing the target values for each covariate included in formula. Ignored with a warning when estimand is not "CATE".

`target.weights` a vector of sampling weights to be applied to `target` when supplied as a data frame. Ignored with a warning when `estimand` is not `"CATE"`.

`contrast` ignored.

`focal` the level of the treatment variable to be considered "focal" (i.e., the "treated" level when `estimand = "ATT"` or the control level when `estimand = "ATC"`). Ignored when `estimand` is `"ATE"` or `"CATE"`. For binary treatments, this generally does not need to be supplied.

Details

`lmw_iv()` computes weights that make the weighted difference in outcome means between the treatment groups equal to the two-stage least squares (2SLS) estimate of the treatment effect. `formula` corresponds to the second-stage (reduced form) model, with the treatment replaced by its fitted values resulting from the first stage model. The first stage is fit by replacing the treatment in the supplied `formula` with the IVs named in `iv` and using the treatment as the outcome. The treatment is assumed to be endogenous and the supplied instrumental variables assumed to be instruments conditional on the other covariates, which are assumed to to be exogenous.

When any treatment-by-covariate interactions are present in `formula` or when `method = "MRI"`, covariates are centered at specific values to ensure the resulting weights correspond to the desired estimand as supplied to the `estimand` argument. For the ATE, the covariates are centered at their means in the full sample. For the ATT and ATC, the covariates are centered at their means in the treatment or control group (i.e., the `focal` group), respectively. For the CATE, the covariates are centered according to the argument supplied to `target` (see below). Note that when covariate-by-covariate interactions are present, they will be centered after computing the interaction rather than the interaction being computed on the centered covariates unless `estimand = "CATE"`, in which case the covariates will be centered at the values specified in `target` prior to involvement in interactions. Note that the resulting effect estimate does not actually correspond to the estimand supplied unless all effect heterogeneity is due to the included covariates.

When treatment-by-covariate interactions are included in `formula`, additional instruments will be formed as the product of the supplied IVs and the interacting covariates. When `method = "MRI"`, instruments will be formed as the product of the supplied IVs and each of the covariates. All treatment-by-covariate interactions are considered endogenous.

Base weights and sampling weights:

Base weights (`base.weights`) and sampling weights (`s.weights`) are similar in that they both involve combining weights with an outcome regression model. However, they differ in a few ways. Sampling weights are primarily used to adjust the target population; when the outcome model is fit, it is fit using weighted least squares, and when target balance is assessed, it is assessed using the sampling weighted population as the target population. Centering of covariates in the outcome model is done using the sampling weighted covariate means. Base weights are primarily used to offer a second level of balancing beyond the implied regression weights, i.e., to fit the 2SLS models in the base-weighted sample. Base weights do not change the target population, so when target balance is assessed, it is assessed using the unweighted population as the target population.

Some forms of weights both change the target population and provide an extra layer of balancing, like propensity score weights that target estimands other than the ATT, ATC, or ATE (e.g., overlap weights), or matching weights where the target population is defined by the matching

(e.g., matching with a caliper, cardinality matching, or coarsened exact matching). Because these weights change the target population, they should be supplied to `s.weights` to ensure covariates are appropriately centered. In `lmw_iv()`, whether weights are supplied to `base.weights` or `s.weights` will not matter for the estimation of the weights but will affect the target population in balance assessment.

When both `base.weights` and `s.weights` are supplied, e.g., when the base weights are the result of a propensity score model fit with sampling weights, it is assumed the base weights do not incorporate the sampling weights; that is, it is assumed that to estimate a treatment effect *without* regression adjustment, the base weights and the sampling weights would have to be multiplied together. This is true, for example, for the weights in a `matchit` or `weightit` object (see below) but not for weights in the output of `MatchIt::match.data()` unless called with `include.s.weights = FALSE` or weights resulting from `CBPS::CBPS()`.

2SLS after using MatchIt or WeightIt: Instrumental variable regression weights can be computed in a matched or weighted sample by supplying a `matchit` or `weightit` object (from **MatchIt** or **WeightIt**, respectively) to the `obj` argument of `lmw()`. The estimand, base weights, and sampling weights (if any) will be taken from the supplied object and used in the calculation of the implied regression weights, unless these have been supplied separately to `lmw_iv()`. The `weights` component of the supplied object containing the matching or balancing weights will be passed to `base.weights` and the `s.weights` component will be passed to `s.weights`. Arguments supplied to `lmw_iv()` will take precedence over the corresponding components in the `obj` object.

Multi-category treatments: Multi-category treatments are not currently supported for `lmw_iv()`.

Fixed effects: A fixed effects variable can be supplied to the `fixef` argument. This is equivalent to adding the fixed effects variable as an exogenous predictor that does not interact with the treatment, IV, or any other covariate. The difference is that computation is much faster when the fixed effect has many levels because demeaning is used rather than including the fixed effect variable as a collection of dummy variables. When using URI, the weights will be the same regardless of whether the fixed effect variable is included as a covariate or supplied to `fixef`; when using MRI, results will differ because the fixed effect variable does not interact with treatment. The fixed effects variable will not appear in the `summary.lmw()` output (but can be added using `addlvariables` argument) or in the model output of `lmw_est()` or `summary.lmw_est()`. Because it does not interact with the treatment, the distribution of the fixed effect variable may not correspond to the target population, so caution should be used if it is expected the treatment effect varies across levels of this variable (in which case it should be included as a predictor). Currently only one fixed effect variable is allowed.

Value

An `lmw_iv` object, which inherits from `lmw` objects and contains the following components:

`treat`	the treatment variable, given as a factor.
`weights`	the computed implied regression weights.
`covs`	a data frame containing the covariates included the model formula.
`estimand`	the requested estimand.
`method`	the method used to estimate the weights (`"URI"` or `"MRI"`).
`base.weights`	the weights supplied to `base.weights`.

s.weights	the weights supplied to s.weights.
call	the original call to lmw_iv().
fixef	the fixed effects variable if supplied to fixef.
formula	the model formula.
iv	the instrumental variables, given as a one-sided formula.
target	the supplied covariate target values when estimand = "CATE", after some initial processing.
contrast	the contrasted treatment groups.
focal	the focal treatment levels when estimand is "ATT" or "ATC".

All functions that lack a specific lmw_iv method work with lmw_iv objects as they do for lmw objects, such as summary.lmw(), plot.lmw(), etc.

References

Chattopadhyay, A., & Zubizarreta, J. R. (2023). On the implied weights of linear regression for causal inference. *Biometrika*, 110(3), 615–629. doi:10.1093/biomet/asac058

See Also

summary.lmw() for summarizing balance and representativeness; plot.lmw() for plotting features of the weights; lmw_est() for estimating treatment effects from lmw_iv objects; influence.lmw() for influence measures; ivreg() in the **ivreg** package for fitting 2SLS models.

Examples

```
# URI for the ATT using instrument `Ins`
lmw.out <- lmw_iv(~ treat + age + education + race +
                    re74, data = lalonde,
                  estimand = "ATT", method = "URI",
                  treat = "treat", iv = ~Ins)
lmw.out
summary(lmw.out, addlvariables = ~married + re75)
```

---

plot.lmw *Plots diagnosing regression-implied weights*

Description

Produces plots to diagnose properties of the weights, including their distribution, to what degree the distribution of covariates involves extrapolation in the weighted sample, and how much influence each unit has on the effect estimate.

Usage

```
## S3 method for class 'lmw'
plot(x, type = "weights", ...)
```

Arguments

x	an lmw object; the output of a call to lmw().
type	the type of plot to display. Allowable options include "weights", "extrapolation", and "influence". See Details. Abbreviations allowed.
...	further arguments passed to specific types of plots. When type = "weights", the following are accepted: rug logical; whether to display a rug plot of the weights. Default is TRUE. mean whether to display a red line indicating the mean of the weights. Default is TRUE. ess whether to display the original and weighted effective sample size in the top right corner. Default is TRUE. Other arguments are passed to density(). When type = "extrapolation", the following are accepted: variables required; a right-sided formula or character vector containing the names of the covariates for which extrapolation is to be assessed. data an optional data frame containing the variables named in variables. When type = "influence", the following are accepted: outcome the name of the outcome variable. Can be supplied as a string containing the name of the outcome variable or as the outcome variable itself. If not supplied, the outcome variable in the formula supplied to lmw(), if any, will be used. data an optional data frame containing the outcome variable named in outcome. id.n the number of points to be labelled in the plot, starting with the most extreme.

Details

When type = "weights", plot.lmw() produces a density plot of the weights within each treatment group. By construction, these weights will have a mean of 1. Some weights may be negative. The effective sample size (ESS) and original sample size (N) will be displayed in the upper right corner of the plot when ess = TRUE.

When type = "extrapolation", plot.lmw() produces a plot of the distribution of weights and covariates for each treatment group. Each dot represents a unit, with values arranged on the x-axis according to their covariate value and the size of the dots corresponding to the magnitude of the weight. Units with positive weights are displayed in black in the upper portion of the plot, and units with negative weights are displayed in red in the lower portion. Having many and large red points indicates a high degree of extrapolation. All points are equally transparent, so darker regions indicate multiple points with the same value. The vertical lines indicates the weighted mean of the covariate in each group, and the X indicates the mean of the covariate in the target sample as determined by the estimand argument in the original call to lmw(). A large discrepancy between the vertical lines and Xs indicates a lack of balance between the treatment group and target sample. When estimand = "CATE" in the original call to lmw(), any variables supplied to variables that were not given a target value will not have the target mean displayed.

When type = "influence", plot.lmw() produces a plot of the scaled sample influence curve (SIC) for each unit by index. It does so by calling influence.lmw(), which fits the outcome model to

extract residuals and compute the SIC as `SIC = (N-1) * w * r / (1 - h)`, where `N` is the sample size, `w` are the units' implied regression weights, `r` are the residuals, and `h` are the hat values. SIC values are scaled to have a maximum of 1. Higher values indicate greater relative influence.

Value

A plot is displayed, and `x` is invisibly returned.

See Also

`lmw()`, `summary.lmw()`, `plot.summary.lmw()`

Examples

```
data("lalonde")

# URI regression for ATT
lmw.out1 <- lmw(~ treat + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                estimand = "ATT", method = "URI",
                treat = "treat")
lmw.out1

# Distribution of weights
plot(lmw.out1, type = "weights")

# Extrapolation/representativeness for age and married
plot(lmw.out1, type = "extrapolation",
     variables = ~age + married)

# Extrapolation/representativeness for race
plot(lmw.out1, type = "extrapolation",
     variables = ~race)

# Influence for re78 outcome
plot(lmw.out1, type = "influence", outcome = "re78")
```

`plot.lmw_est` *Plot diagnostics for an* `lmw_est` *object*

Description

Produces plots to diagnose the regression model fit to estimate the treatment effect. These include an influence plot based on the sample influence curve (SIC) and the regression diagnostics plots available for `lm` objects in `plot.lm()`.

Usage

```
## S3 method for class 'lmw_est'
plot(x, type = "influence", ...)
```

Arguments

x	an lmw_est object; the output of a call to lmw_est().
type	the type of plot to display. Allowable options include "influence" and "lm". See Details. Abbreviations allowed.
...	When type = "influence", the following are accepted:
	outcome the name of the outcome variable. Can be supplied as a string containing the name of the outcome variable or as the outcome variable itself. If not supplied, the outcome variable in the formula supplied to lmw(), if any, will be used.
	data an optional data frame containing the outcome variable named in outcome.
	id.n the number of points to be labelled in the plot, starting with the most extreme.
	When type = "lm", any arguments passed to plot.lm() are accepted and passed directly to plot.lm.

Details

When type = "influence", plot.lmw_est() produces a plot of the scaled sample influence curve (SIC) for each unit by index. It does so by calling influence.lmw_est(), which extract the model residuals and computes the SIC as SIC = (N-1) * w * r / (1 - h), where N is the sample size, w are the units' implied regression weights, r are the residuals, and h are the hat values. SIC values are scaled to have a maximum of 1. Higher values indicate greater relative influence.

When type = "lm", plot.lmw_est() produces several plots displayed sequentially according to the arguments supplied to plot(). These plots are produced by plot.lm() to diagnose the distribution of residuals and other measures of leverage and influence.

Value

A plot is displayed, and x is invisibly returned.

See Also

lmw_est(), influence.lmw_est(), plot.lm()

Examples

```
data("lalonde")

# URI regression for ATT
lmw.out1 <- lmw(~ treat + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                estimand = "ATT", method = "URI",
                treat = "treat")

lmw.fit1 <- lmw_est(lmw.out1, outcome = "re78")
lmw.fit1

# Influence using SIC
```

```
plot(lmw.fit1, type = "influence")

# Usual regression diagnostics
plot(lmw.fit1, type = "lm", which = 1)
```

`plot.summary.lmw` *Produce a Love plot of balance statistics*

Description

Produces Love plots (also known as dot plots) of balance statistics to summarize balance visually. The plots are generated using `dotchart()` and `points()`.

Usage

```
## S3 method for class 'summary.lmw'
plot(
  x,
  stats,
  abs = TRUE,
  var.order = "data",
  threshold = NULL,
  layout = "vertical",
  ...
)
```

Arguments

`x`	a `summary.lmw` object; the output of a call to `summary.lmw()` with `standardize = TRUE`.
`stats`	a vector of the names of the columns in the `summary.lmw` output to plot; more than one is allowed. Abbreviations allowed. When unspecified, the TSMD statistics for each treatment group will be plotted.
`abs`	`logical`; whether the statistics should be plotted in absolute value (`TRUE`) or not (`FALSE`). Default is `TRUE`. This does not affect the display of KS statistics (which are always non-negative). When `TRUE` and standardized mean differences are displayed, the x-axis title will be "TASMD", i.e., target absolute standardized mean difference.
`var.order`	how the variables should be ordered. Allowable options include `"data"`, ordering the variables as they appear in the summary output, `"alphabetical"`, ordering the variables alphabetically, and, when `un = TRUE` in the call to `summary.lmw()`, `"unadjusted"`, ordering the variables by the first statistic in `stats` in the unadjusted sample. Default is `"data"`. Abbreviations allowed.
`threshold`	numeric values at which to place vertical lines indicating a balance threshold. These can make it easier to see for which variables balance has been achieved given a threshold. Multiple values can be supplied to add multiple lines. When

	abs = FALSE, the lines will be displayed on both sides of zero. The lines are drawn with abline with the linetype (lty) argument corresponding to the order of the entered variables (see options at par()). Enter a value as NA to skip that value of lty (e.g., c(NA, .05) to have only a dashed vertical line at .05).
layout	how the multiple plots should be laid out. Allowable options include "vertical" (the default) and "horizontal". Abbreviations allowed.
...	further arguments passed to dotplot().

Details

Love plots will be produced for the requested statistics in the summary.lmw output. How these plots are arranged depends on the value supplied to layout, which uses layout() to arrange the plots.

Value

A plot is displayed, and x is invisibly returned.

See Also

summary.lmw()

Examples

```
data("lalonde")

# URI regression for ATT
lmw.out1 <- lmw(~ treat + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                estimand = "ATT", method = "URI",
                treat = "treat")
lmw.out1
(s <- summary(lmw.out1))

plot(s)
plot(s, stats = "SMD", abs = FALSE)
```

---

summary.lmw *Assess balance for an* lmw *object*

Description

Computes balance statistics for an lmw object created by lmw(). Balance involves not only the similarity between the treatment groups but also the similarity between each treatment group and the target population.

Usage

```
## S3 method for class 'lmw'
summary(
  object,
  un = TRUE,
  addlvariables = NULL,
  standardize = TRUE,
  data = NULL,
  stat = "balance",
  ...
)

## S3 method for class 'lmw_multi'
summary(
  object,
  un = TRUE,
  addlvariables = NULL,
  standardize = TRUE,
  data = NULL,
  contrast = NULL,
  stat = "balance",
  ...
)

## S3 method for class 'summary.lmw'
print(x, digits = max(3, getOption("digits") - 4), ...)
```

Arguments

`object`	an `lmw` object; the output of a call to `lmw()`.
`un`	`logical`; whether to display balance statistics for the sample prior to weighting and, additionally, with base weights applied (if supplied). If `s.weights` were supplied to `lmw()`, the unadjusted sample will be weighted by the sampling weights.
`addlvariables`	additional variables for which balance statistics are to be computed along with the covariates in the `lmw` object. Can be entered in one of three ways: as a data frame of covariates with as many rows as there were units in the original `lmw()` call, as a string containing the names of variables in `data`, or as a right-sided formula with the additional variables (and possibly their transformations) found in `data`, the environment, or the `lmw` object.
`standardize`	`logical`; whether to compute standardized (`TRUE`) or unstandardized (`FALSE`) mean differences. Default is `TRUE`.
`data`	a optional data frame containing variables named in `addlvariables` if specified as a string or formula.
`stat`	`character`; whether to display balance statistics (i.e., standardized mean differences and Kolmogorv-Smirnov statistics; `"balance"`) or distribution statistics

	(i.e., means and standard deviations; "distribution"). Default is "balance". Abbreviations allowed.
...	ignored.
contrast	for multi-category treatments with method = "MRI", which two groups should be compared. If NULL, only target balance statistics will be displayed. Ignored with binary treatments or when method = "URI".
x	a summary.lmw object.
digits	the number of digits to print.

Details

summary.lmw() produces covariate balance or distribution statistics and effective samples sizes before and after adjustment by the regression weights and base weights, if supplied. For each covariate, the following balance statistics are computed when stat = "balance":

- SMD - the standardized mean difference (SMD) between the treated and control groups
- TSMD Treated - the target standardized mean difference (TSMD) between the treated group and target sample
- TSMD Control - the TSMD between between the control group and target sample
- KS - the Kolmogorov-Smirnov (KS) statistic between the treated and control groups
- TKS Treated - the target KS (TKS) statistic between the treated group and target sample
- TKS Control - the TKS statistic between the control group and target sample

For multi-category treatments with method = "MRI", balance statistics are are computed between each treatment group and the target sample.

When stat = "distribution" the mean and standard deviation of each covariate is compute before and after adjustment and for the target sample. (Standard deviations are printed in parentheses for visual clarity.)

After weighting with the regression weights, the mean difference between the treated and control groups of each covariate included in the original call to lmw() will be equal to zero. However, the mean difference between each treatment group and the target sample may not be equal to zero when method = "URI" in the call to lmw(), and covariates supplied to addlvariables not included in the call to lmw() may not be well balanced.

When s.weights are supplied to lmw(), the unadjusted statistics (if requested) will incorporate the sampling weights. When base.weights are supplied to lmw(), the unadjusted statistics will *not* incorporate the base weights; rather, balance with base weights applied (if supplied) will be produced in a separate balance table (see Value below).

SMDs are computed as the difference between the (weighted) means divided by a standardization factor, which is the standard deviation of the covariate in the target sample. When estimand = "ATT" in the call to lmw(), the standardization factor is the standard deviation in the treated group; when estimand = "ATC", the standardization factor is the standard deviation in the control group; when estimand = "ATE" or when estimand = "CATE" and a target profile is supplied, the standardization factor is the square root of the average of the variances of both treatment groups; when estimand = "CATE" and a target dataset is supplied, the standardization factor is the standard deviation in the target dataset. When s.weights is supplied, the standardization factor is computed including the sampling weights; otherwise it is computed in the unweighted sample.

For binary covariates, the KS statistic is equal to the unstandardized difference in means and is computed as such.

When `estimand = "CATE"` in the original call to `lmw()`, any variables supplied to `addlvariables` that were not given a target value will not have any target statistics computed (e.g., TSMD, TKS, target means, etc.).

The effective sample size (ESS) is computed within each group as $(\sum w)^2 / \sum w^2$. With uniform weights, this is equal to the sample size.

Value

A `summary.lmw` object, which contains the following components:

`call` The original call to `lmw()`.

`nn` The (effective) sample sizes before and after weighting.

`bal.un` When `stat = "balance"` and `un = TRUE`, the balance statistics prior to weighting.

`bal.base.weighted` When `stat = "balance"`, `un = TRUE` and base weights were supplied to `lmw()`, the balance statistics with the base weights applied.

`bal.weighted` When `stat = "balance"`, the balance statistics with the implied regression weights applied.

`dist.un` When `stat = "distribution"` and `un = TRUE`, the distribution statistics prior to weighting.

`dist.base.weighted` When `stat = "distribution"`, `un = TRUE` and base weights were supplied to `lmw()`, the distribution statistics with the base weights applied.

`dist.weighted` When `stat = "distribution"`, the distribution statistics with the implied regression weights applied.

`method` The method used to estimate the weights (i.e., URI or MRI)

`base.weights.origin` If base weights were supplied through the `obj` argument to `lmw()`, their origin (i.e, **MatchIt** or **WeightIt**)

With multi-category treatments and `method = "MRI"`, the object will also inherit from class `summary.lmw_multi`.

See Also

`lmw()` for computing the implied regression weights, `plot.summary.lmw()` for plotting the balance statistics in a Love plot, `plot.lmw()` for assessing the representativeness and extrapolation of the weights

Examples

```
data("lalonde")

# URI regression for ATT
lmw.out1 <- lmw(~ treat + age + education + race + married +
```

```
                  nodegree + re74 + re75, data = lalonde,
                  estimand = "ATT", method = "URI",
                  treat = "treat")

lmw.out1

summary(lmw.out1)

summary(lmw.out1, stat = "distribution")

# Adding additional variables to summary, removing unweighted
summary(lmw.out1, un = FALSE,
        addlvariables = ~I(age^2) + I(nodegree*re74))


# MRI regression for ATT after PS matching
m.out <- MatchIt::matchit(treat ~ age + education + race + married +
                            nodegree + re74 + re75,
                          data = lalonde, method = "nearest",
                          estimand = "ATT")

lmw.out2 <- lmw(~ treat + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                method = "MRI", treat = "treat", obj = m.out)

lmw.out2

summary(lmw.out2)

# MRI for a multi-category treatment ATE
lmw.out3 <- lmw(~ treat_multi + age + education + race + married +
                  nodegree + re74 + re75, data = lalonde,
                estimand = "ATE", method = "MRI",
                treat = "treat_multi")

lmw.out3

summary(lmw.out3)

summary(lmw.out3, contrast = c("2", "1"))
```

`summary.lmw_est_aipw` *Extract effect estimates and standard errors from* `lmw_est` *fits*

Description

`summary()` computes the treatment effect and potential outcome mean estimates from the supplied `lmw_est` object. It functions similarly to `summary.lm()` in producing estimate tables with the estimates, standard errors, t-statistics, and p-values. Other model statistics can be additionally requested.

Usage

```
## S3 method for class 'lmw_est_aipw'
summary(object, model = FALSE, ci = TRUE, alpha = 0.05, ...)

## S3 method for class 'lmw_est'
summary(object, model = FALSE, ci = TRUE, alpha = 0.05, ...)
```

Arguments

object	an lmw_est object; the output of a call to lmw_est.
model	logical; whether to produce a coefficient table for the outcome model coefficients. Note that these values should not be interpreted or reported so they are not produced by default.
ci	logical; whether to include confidence intervals in the output.
alpha	when ci = TRUE, the alpha value used to compute the critical test statistic for the confidence interval; equivalently, 1 minus the confidence level (e.g., for a 99% confidence interval, alpha = .01 should be specified). Default is .05 for a 95% confidence interval.
...	ignored.

Details

summary.lmw_est() produces a table of treatment effect estimates corresponding to all possible pairwise contrasts between the treatment levels. These treatment effects generalize to the population implied by the regression weights, which depends on the supplied estimand, whether sampling weights were provided, and which of the MRI or URI models was requested. The treatment effects are computed using linear contrasts of the outcome model coefficients.

When method = "MRI", the potential outcome mean estimates are also reported. These correspond to the potential outcome means in the population implied by the regression weights. When method = "URI", only the treatment effects are estimated; the model-implied outcome means do not correspond to the potential outcome means for the population implied by the regression weights. That is, while the treatment effect generalizes to the population defined by the regression weights, the estimated potential outcome means do not and so are not reported.

When model = TRUE, the model coefficients and their tests statistics are additionally produced. It is inappropriate to interpret or report these values as they have no causal interpretation. This is especially true when using AIPW, as the model coefficients do not incorporate the augmentation terms.

Value

A summary.lmw_est object with the following components:

call	the original call to lmw_est()
means	a matrix containing the estimated potential outcome means, their standard errors, confidence interval limits (if requested with ci = TRUE), t-statistics, and p-values. Omitted when method = "URI" or fixef is not NULL and for lmw_iv objects.

`coefficients` a matrix containing the treatment effect estimates and their standard errors, t-statistics, and p-values.When `ci = TRUE`, the confidence limits `"95% CI L"` (lower) and `"95% CI U"` (upper) will be included between the standard error and t-statistic columns. When AIPW is used, z-statistics and z-tests are reported instead.

`model.coefficients`
when `model = TRUE`, the coefficient table of the model coefficients, which has the same columns as `coefficients`.

`aliased` when `model = TRUE`, a named logical vector showing if the original coefficients are aliased (i.e., `NA`).

`sigma`, `df`, `r.squared`, `adj.r.squared`
the residual standard deviation, degrees of freedom components, R-squared, and adjusted R-squared. See `summary.lm()`. When AIPW is used, `sigma` and `df` are omitted.

Other components containing information for printing are also included.

See Also

`lmw_est()` for fitting the outcome regression model, `summary.lm()` for more information on the output components

Examples

```
# See examples at `help("lmw_est")`
```

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